

# Fast Liveness Using DJ Graphs

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# Agenda

- DJ Graphs and Merge Sets
- Top-down Merge Set Computation
- Liveness Analysis – Boissinot et al
- Liveness Analysis using Merge Sets
- Conclusion

# DJ Graphs

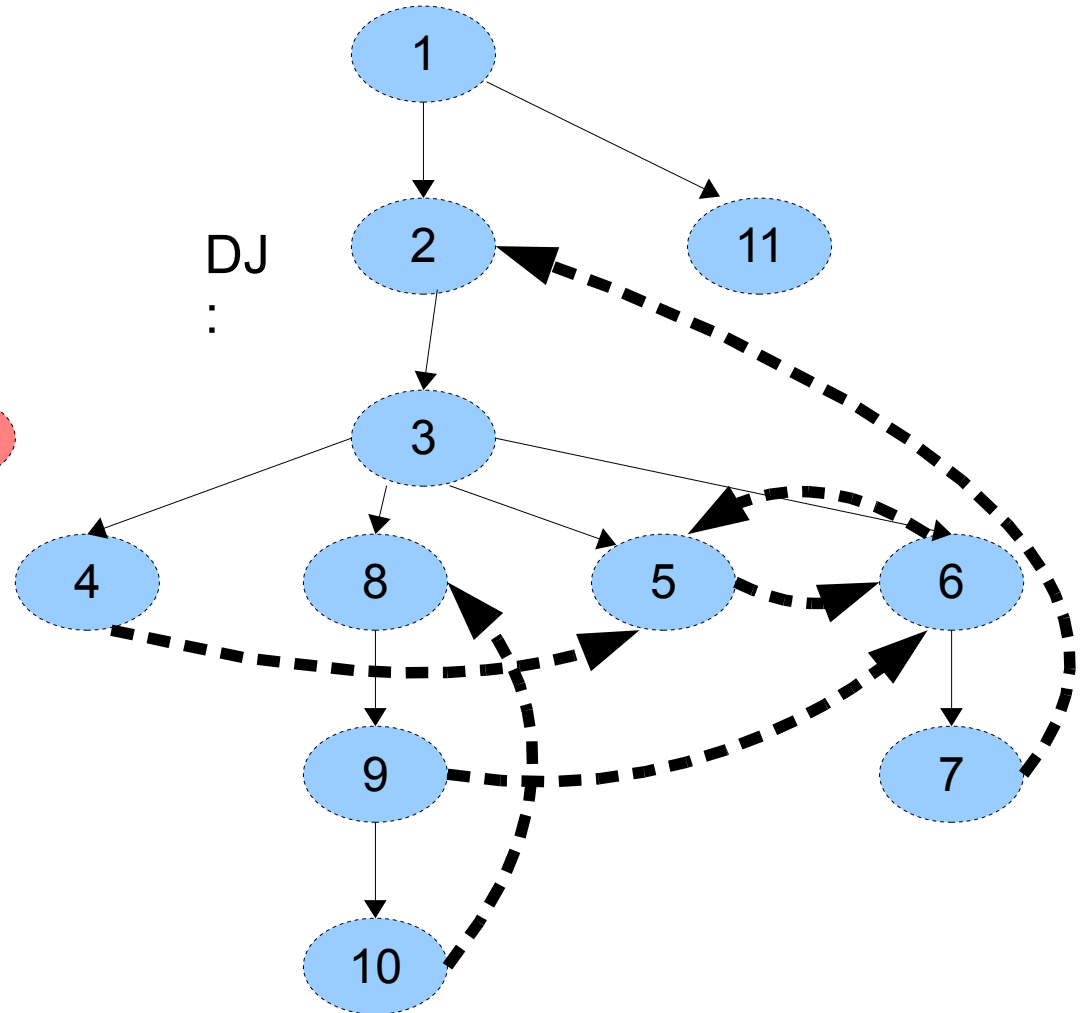
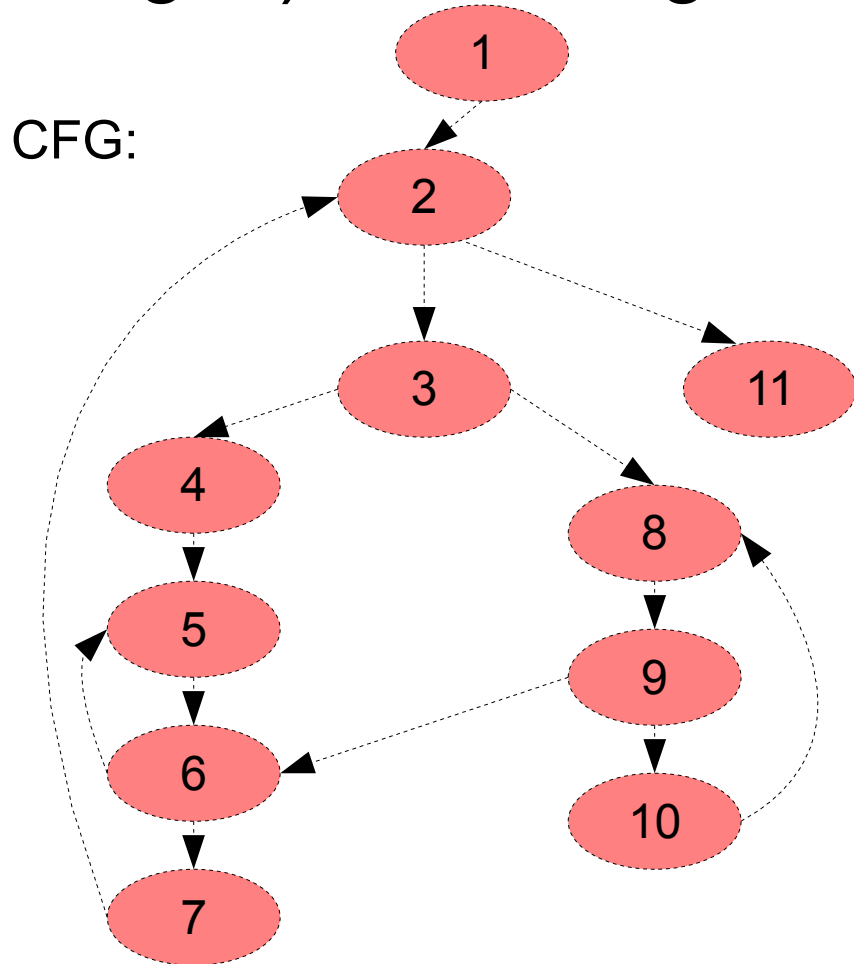
- For a CFG  $G=(V,E)$ , an edge  $e=(s,t)$  is a J-edge when  $s$  does not strictly dominate  $t$ .
- J-edges are a subset of  $E$
- A DJ Graph[Sreedhar POPL '95]  $G_{DJ}=(V,E_{DJ})$  such that

$$- E_{DJ} = E_{D-tree} \cup J$$

$$- E_{DJ} = E \cup E_{D-tree}$$

# DJ Graphs (contd ...)

- DJ Graphs consist of dominator edges (D-edges) and J-edges

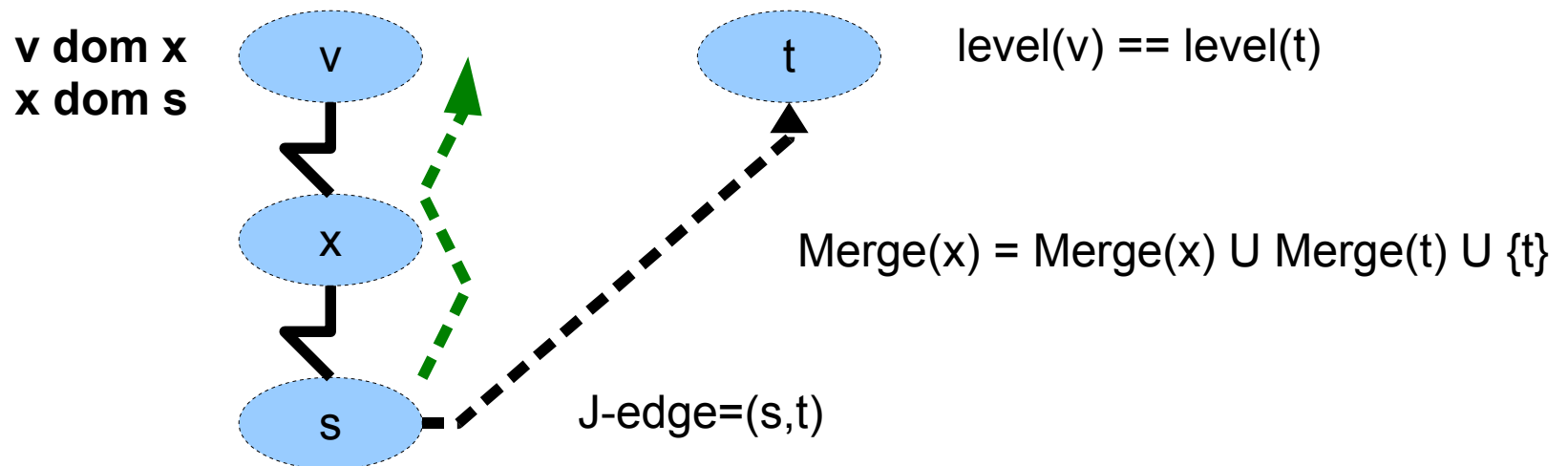


# Merge Set

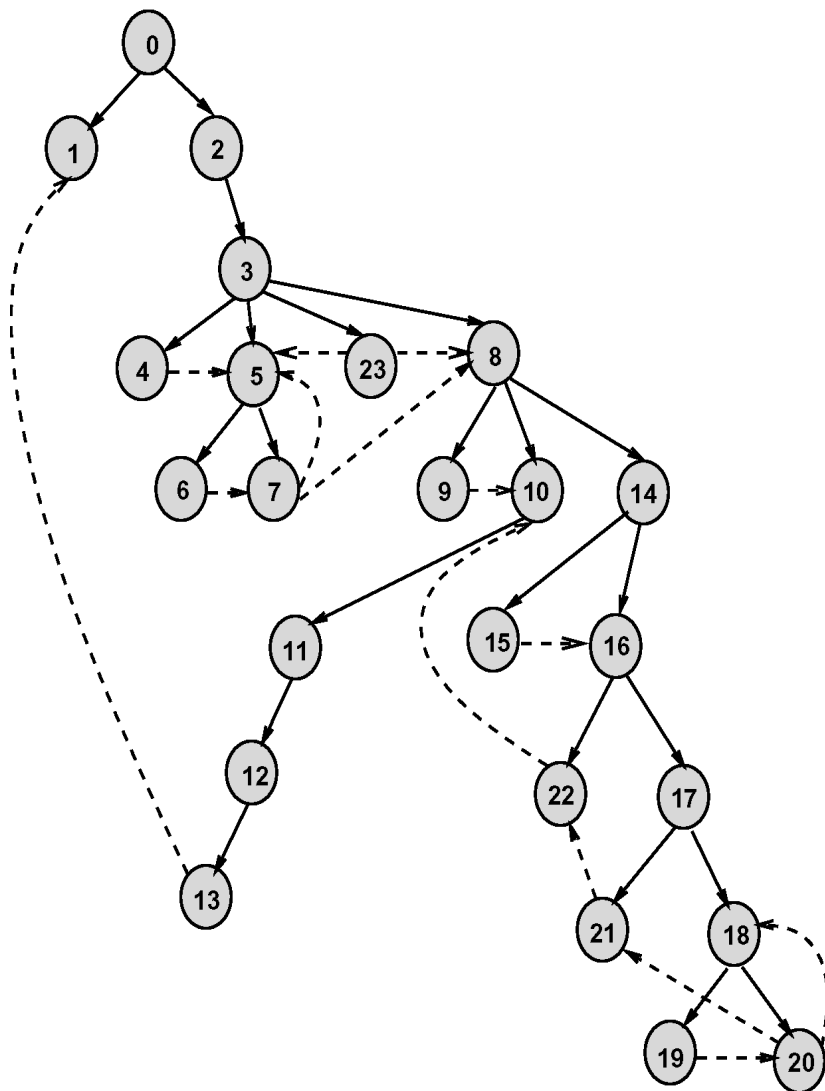
- **Definition:** Merge Set [Pingali et al JACM 2003] of a node  $n$  is the set of nodes, denoted as  $\text{Merge}(n)$ , where a  $\Phi$  needs to be placed if a variable is defined in  $n$ .
- Merge Sets of the nodes in a CFG can be computed, irrespective of where the definitions finally appear.
- The advantages are in re-using  $\text{Merge}(n)$  information when variables are defined in same/similar nodes. As long as the CFG remains unchanged  $\Phi$ -placement can re-use  $\text{Merge}(n)$  information.

# Top-Down Merge Set Computation(TDMSC)

- The algorithm proceeds top-down on the DJ Graph starting at the start node and computing level-by-level [ Das and Ramakrishna TOPLAS 2005 ]
- At each level we look for J-edge= $(s,t)$  targets and update the merge set of each node  $x$  lying between the levels of the source and target in the dominator tree using  $\mathbf{Merge(x) = Merge(x) \cup Merge(t) \cup \{t\}}$ . Implies  $\mathbf{Merge(x) \supseteq Merge(t)}$ .



# TDMSC -an example



Merge(4)	= {5} U Merge(5);	{5,8}
Merge(5)	= {5,8} U Merge(5) U Merge(8);	{5,8}
Merge(6)	= {7} U Merge(7);	{5,7,8}
Merge(7)	= {5,8} U Merge(5) U Merge(8);	{5,8}
Merge(9)	= {10} U Merge(10);	{10}
Merge(14)	= {10} U Merge(10);	{10}
Merge(15)	= {16} U Merge(16);	{10,16}
Merge(16)	= {10} U Merge(10);	{10}
Merge(17)	= {22} U Merge(22);	{10,22}
Merge(18)	= {18,21} U Merge(18) U Merge(21);	{10,18,21,22}
Merge(19)	= {20} U Merge(20);	{10,18,20,21,22}
Merge(20)	= {18,21} U Merge(18) U Merge(21);	{10,18,21,22}
Merge(21)	= {22} U Merge(22);	{10,22}
Merge(22)	= {10} U Merge(10);	{10}
Merge(23)	= {5,8} U Merge(5) U Merge(8);	{5,8}

# Advantages of TDMSC

- Can be applied to any arbitrary CFG – reducible or irreducible
- May require multiple passes(iterative) for the Merge sets to reach respective fixed points
- Analyses using SPEC CPU2000 shows that almost for 80% of cases a single top down pass suffices.



# Liveness Analysis using Merge Sets

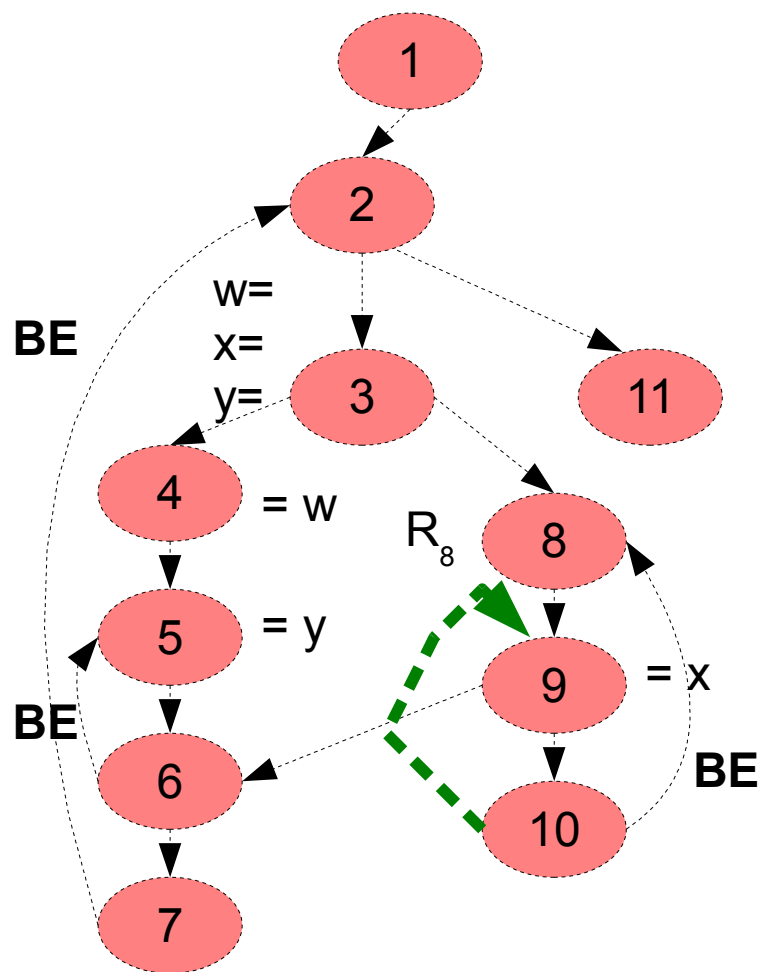
- Merge sets can also be used to compute fast liveness ( proposed by Boissinot et al [CGO 2008] )

# Fast Liveness Analysis

- $\text{IsLiveIn}(v,n)$ : A variable  $v$  is live-in at node  $n$  if there exists a path from  $n$  to a **use** of  $v$  that does not pass through a **def** of  $v$
- $\text{IsLiveIn}$  uses the dominator tree and the  $T_q$  and  $R_q$  sets
- $T_q$  – is the set of target nodes of back-edges in a CFG that “affect” node  $q$
- $R_q$  – is the set of nodes reachable from  $q$  in the back-edge-free CFG

# Fast Liveness Using $T_q$ and $R_q$ – a motivating example

- IsLiveIn(10,x) ?



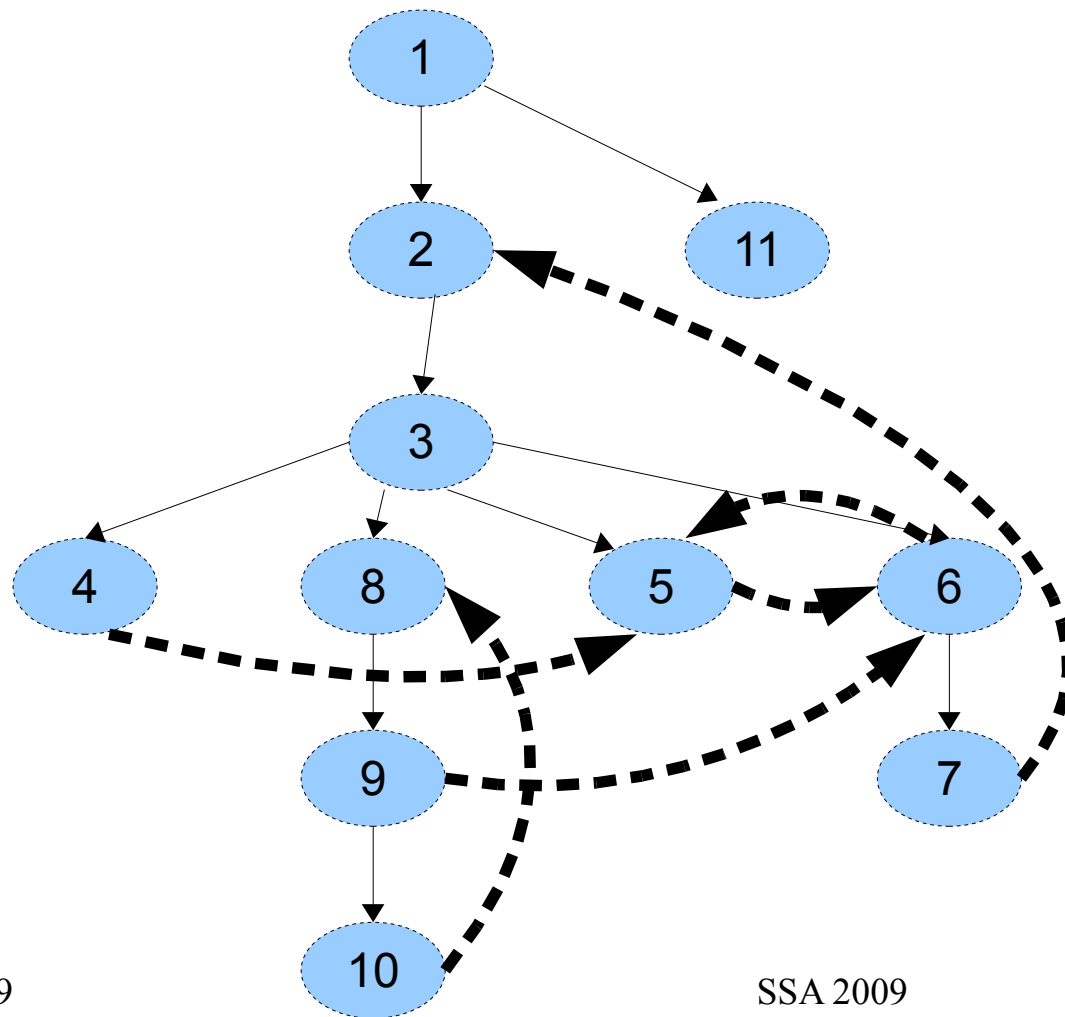
$T_1$	=	{ 1 }
$T_2$	=	{ 2 }
$T_3$	=	{ 2, 3 }
$T_4$	=	{ 2, 4 }
$T_5$	=	{ 2, 5 }
$T_6$	=	{ 2, 5, 6 }
$T_7$	=	{ 2, 7 }
$T_8$	=	{ 2, 5, 8 }
$T_9$	=	{ 2, 5, 8, 9 }
$T_{10}$	=	{ 2, 5, 8, 10 }
$T_{11}$	=	{ 11 }

$$R_9 = \{6, 7, 9, 10\}$$

$$R_7 = \{7\}$$

# The DJ Graph and Merge Sets for the same example

Here are the merge sets for the same example:



Merge(1) =  $\{\}$   
Merge(2) =  $\{ 2 \}$   
Merge(3) =  $\{ 2 \}$   
Merge(4) =  $\{ 2, 5, 6 \}$   
Merge(5) =  $\{ 2, 5, 6 \}$   
Merge(6) =  $\{ 2, 5, 6 \}$   
Merge(7) =  $\{ 2 \}$   
Merge(8) =  $\{ 2, 5, 6, 8 \}$   
Merge(9) =  $\{ 2, 5, 6, 8 \}$   
Merge(10) =  $\{ 2, 5, 6, 8 \}$   
Merge(11) =  $\{\}$

—————> Dominator Edge  
- - - -> J-edge

# How are Merge and $T_q$ related ?

**Observation:** The Merge set of a node  $q$  denoted as  $\text{Merge}(q)$  and  $T_q$  are related by the following formula:

$$T_q - \{q\} \subseteq \text{Merge}(q)$$

$$T_9 = \{2, 5, 8, 9\}, \text{Merge}(9) = \{2, 5, 6, 8\}$$

$$T_9 - \{9\} \subseteq \text{Merge}(9)$$

# IsLiveIn and IsLiveInMergeSet

```
bool IsLiveIn(var a, node q) {  
     $T_{(q,a)} \leftarrow T_q \cap \text{sdom}(\text{def}(a))$   
    // sdom(x) contains all nodes strictly dominated by x  
    for t in  $T_{(q,a)}$  do  
        if  $R_t \cap \text{uses}(a) \neq \Phi$  then return true  
    return false  
}
```

```
bool IsLiveInMergeSet(var a, node q) {  
     $M_{(q,a)} \leftarrow (\text{Merge}(q) \cup \{q\}) \cap \text{sdom}(\text{def}(a))$   
    for t in  $M_{(q,a)}$  do  
        if  $R_t \cap \text{uses}(a) \neq \Phi$  then return true  
    return false  
}
```



IsLiveIn= IsLiveInMergeSet

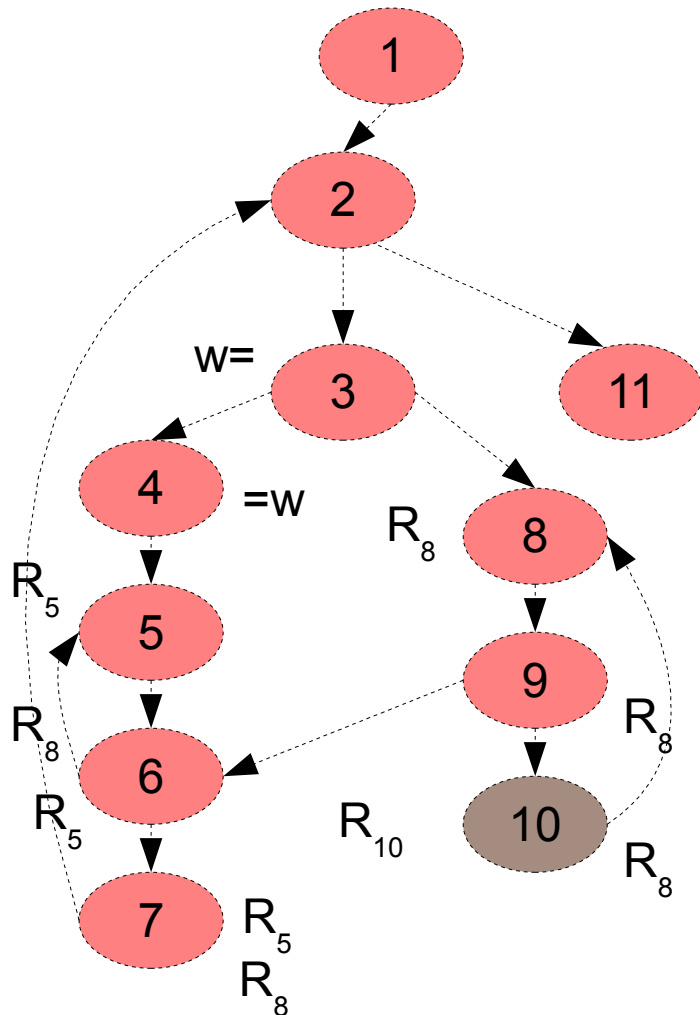
# IsLiveInMergeSetUsingDJGraph

```
bool  IsLiveInMergeSetUsingDJGraph(q,a) {
(1)  M(q,a) ← ( Merge(q) ∪ {q} )
(2)  for t in uses(a) do {
(3)    while ( level(t) != level(def(a)) && t != def(a)) {
(4)      if ( t ∩ M(q,a) )
(5)        return true
(6)      t = dom-parent(t)
        //Climb up from node t in the DJ Graph
(7)    } // end while
(8) } // end for
(9) return false
}
```

IsLiveIn= IsLiveInMergeSetUsingDJGraph

# IsLiveIn vs IsLiveInMergeSetUsingDJGraph

- $\text{IsLiveIn}(10, w) \rightarrow \text{False}$



$$T_{10} = \{2, 5, 8, 10\}$$

$$\begin{aligned} T_{10,w} &= T_{10} \cap \text{sdom}(\text{def}(w)) \\ &= T_{10} \cap \text{sdom}(3) \\ &= \{2, 5, 8, 10\} \cap \{3 \dots 10\} \\ &= \{5, 8, 10\} \end{aligned}$$

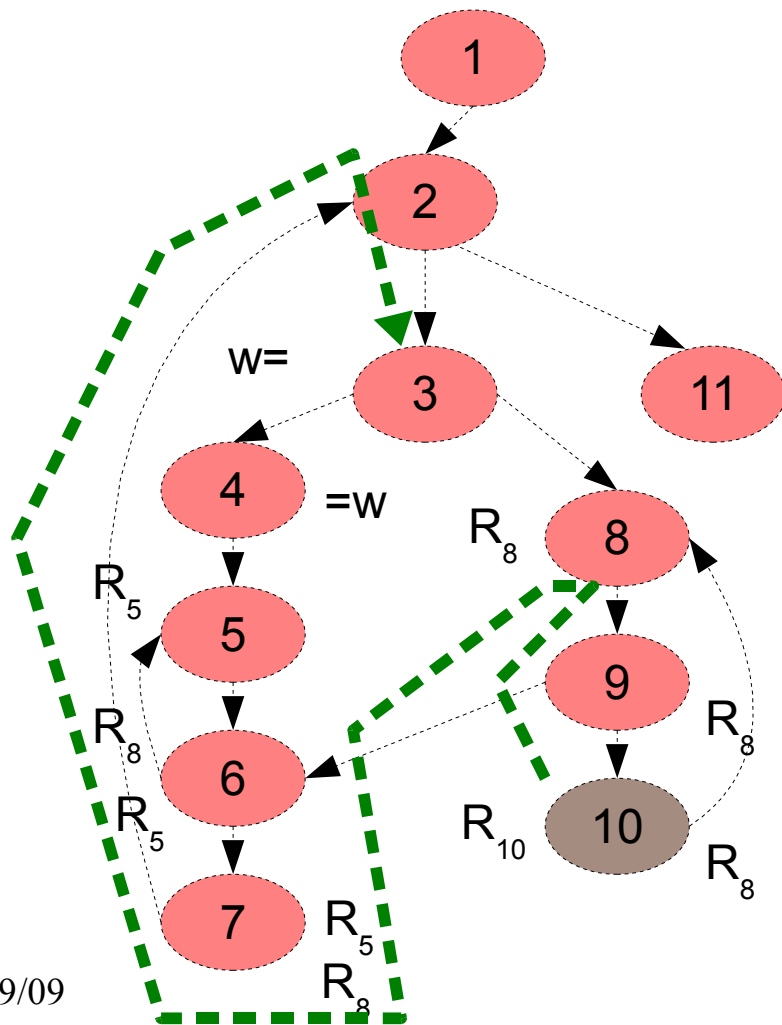
$$\text{uses}(w) = \{4\}$$

$$R_5, R_8, R_{10} \cap \{4\} = \{\}$$



# IsLiveIn vs IsLiveInMergeSetUsingDJGraph

- $\text{IsLiveIn}(10,w) \rightarrow \text{False}$



$$T_{10} = \{2,5,8,10\}$$

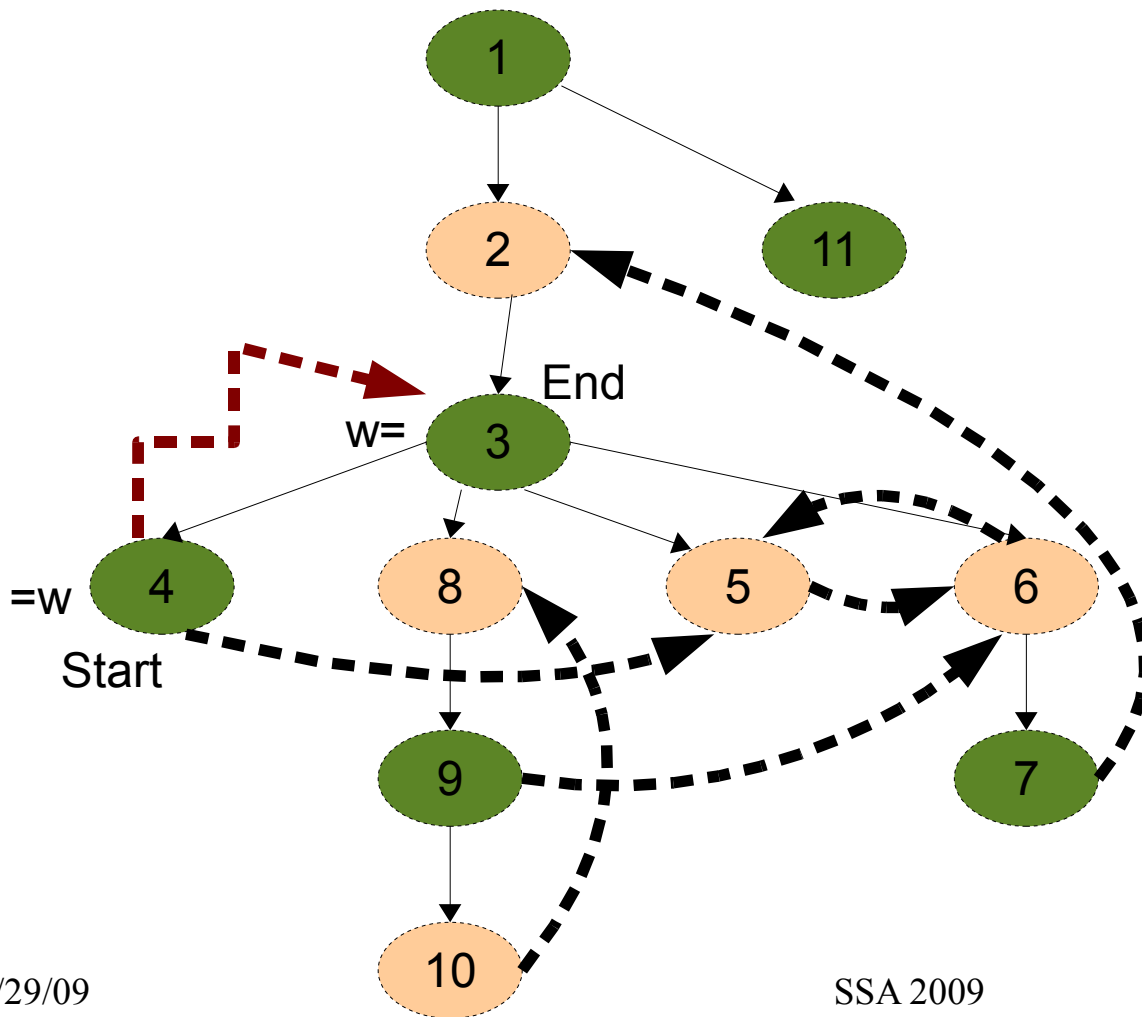
$$\begin{aligned} T_{10,w} &= T_{10} \cap \text{sdom}(\text{def}(w)) \\ &= T_{10} \cap \text{sdom}(3) \\ &= \{2,5,8,10\} \cap \{3 \dots 10\} \\ &= \{5,8,10\} \end{aligned}$$

$$\text{uses}(w) = \{4\}$$

$$R_5, R_8, R_{10} \cap \{4\} = \{\}$$

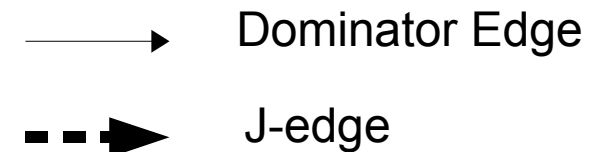
# IsLiveIn vs IsLiveInMergeSetUsingDJGraph

- $\text{IsLiveInMergeSetUsingDJGraph}(10, w) \rightarrow \text{False}$



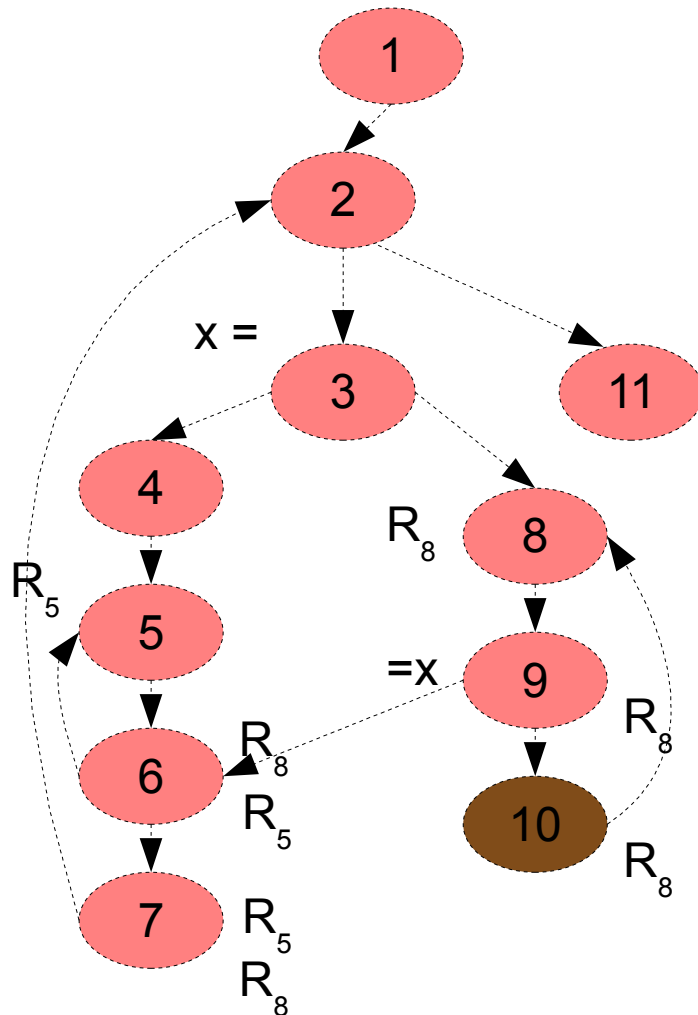
$$\begin{aligned}
 M_{10,w} &= M_{10} \cup \{10\} \\
 &= \{2,5,6,8\} \cup \{10\} \\
 &= \{2,5,6,8,10\}
 \end{aligned}$$

$$\begin{aligned}
 \text{uses}(w) &= \{4\} \\
 \text{def}(w) &= \{3\}
 \end{aligned}$$



# IsLiveIn vs IsLiveInMergeSetUsingDJGraph

- $\text{IsLiveIn}(10,x) \rightarrow \text{True}$



$$T_{10} = \{2,5,8,10\}$$

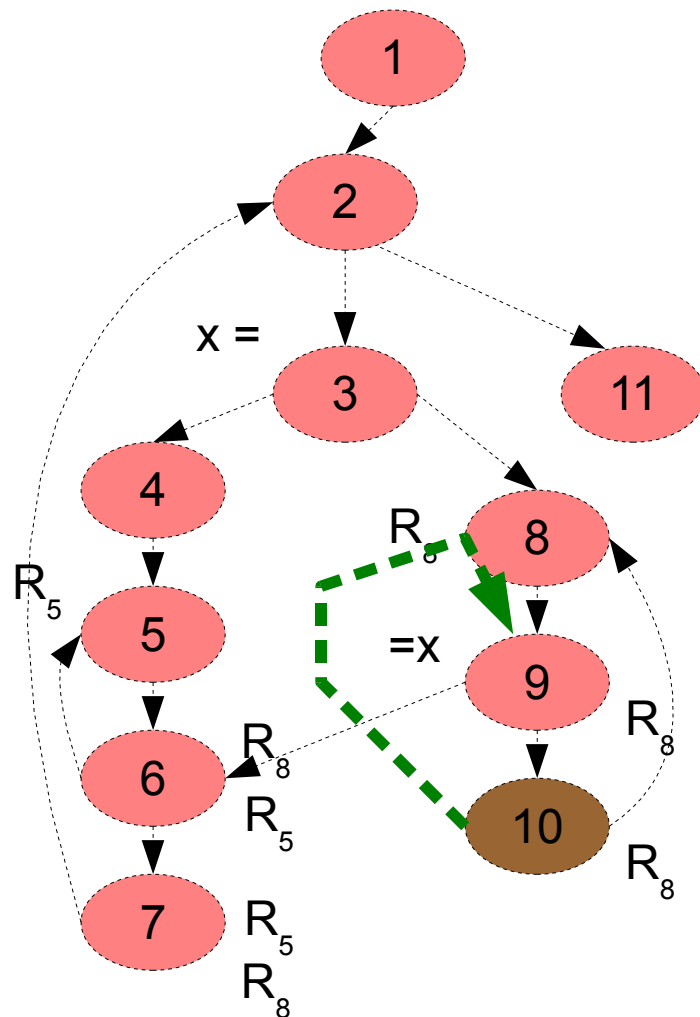
$$\begin{aligned} T_{10,y} &= T_{10} \cap \text{sdom}(\text{def}(x)) \\ &= T_{10} \cap \text{sdom}(3) \\ &= \{2,5,8,10\} \cap \{3 \dots 10\} \\ &= \{5,8,10\} \end{aligned}$$

$$\text{uses}(x) = \{9\}$$

$$R_{10}, R_5, R_8 \cap \{9\} \neq \{\}$$

# IsLiveIn vs IsLiveInMergeSetUsingDJGraph

- $\text{IsLiveIn}(10,x) \rightarrow \text{True}$



$$T_{10} = \{2,5,8\}$$

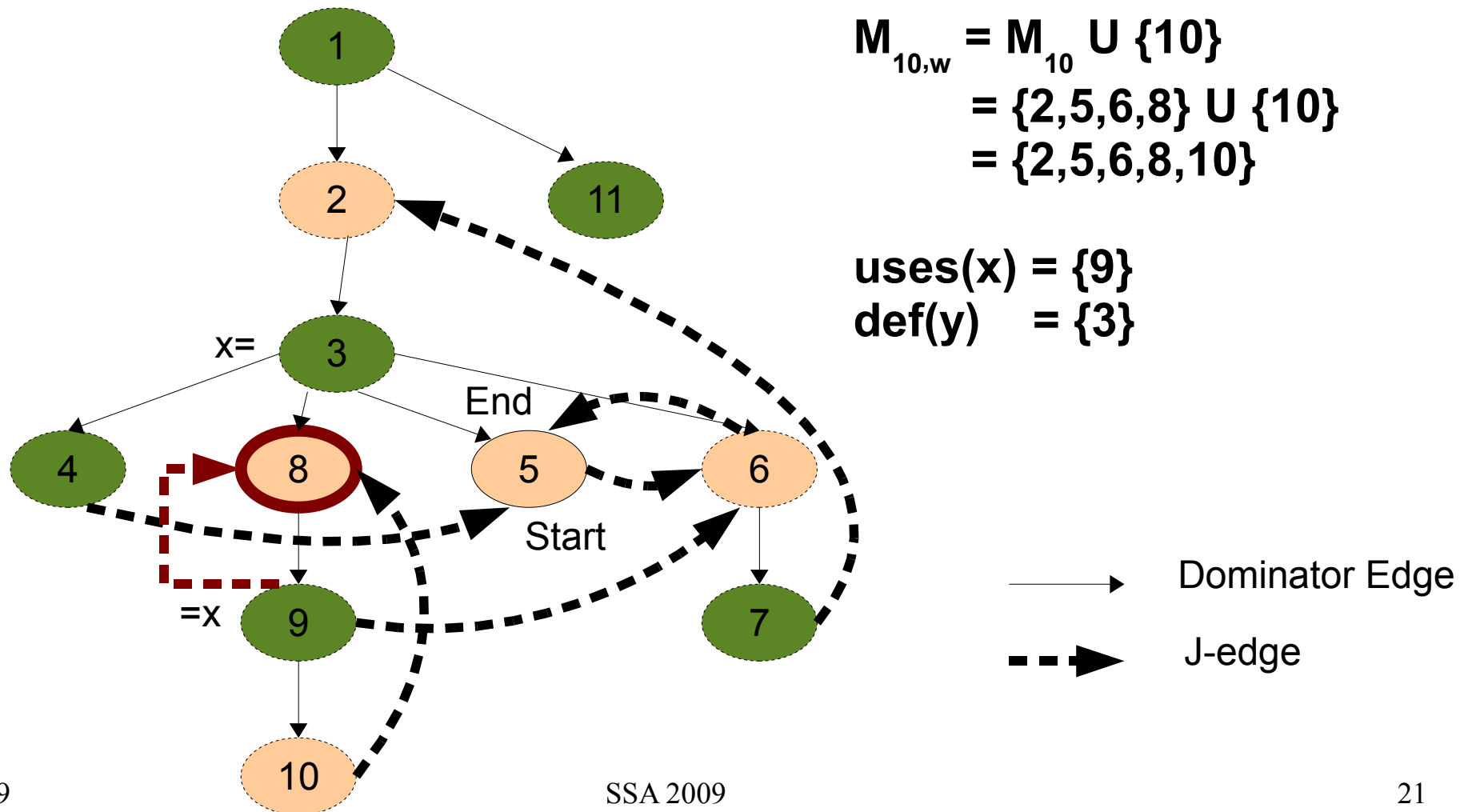
$$\begin{aligned} T_{10,x} &= T_{10} \cap \text{sdom}(\text{def}(x)) \\ &= T_{10} \cap \text{sdom}(3) \\ &= \{2,5,8,10\} \cap \{3 \dots 10\} \\ &= \{5,8,10\} \end{aligned}$$

$$\text{uses}(x) = \{9\}$$

$$R_{10}, R_5, R_8 \cap \{9\} \neq \{\}$$

# IsLiveIn vs IsLiveInMergeSetUsingDJGraph

- $\text{IsLiveInMergeSetUsingDJGraph}(10, x) \rightarrow \text{True}$



# Conclusion

- New algorithm for handling Liveness Analysis using DJ Graphs
- Simplified handling via the usage of Merge Sets
  - removes the need of computing  $T_q$  and  $R_q$  sets
- Merge Sets can be computed easily for both reducible and irreducible graphs efficiently